

Music & Cognition

11/14

www.hum.uva.nl/mmm (see under 'Related Courses')

Today

- Homework Evaluation
- Application of Probability to Music research
- A Gentle Introduction to Probability

Who's this bloke?

- Researcher on the EmCAP project with Olivia and Henkjan.
- <http://www.science.uva.nl/~lsmith>

EU Project: *Emergent Cognition through Active Perception (EmCAP)*

(European Commission FP6-IST, contract 013123)

- The study of how cognitive behaviour in artificial systems can emerge through interacting with a musical environment.

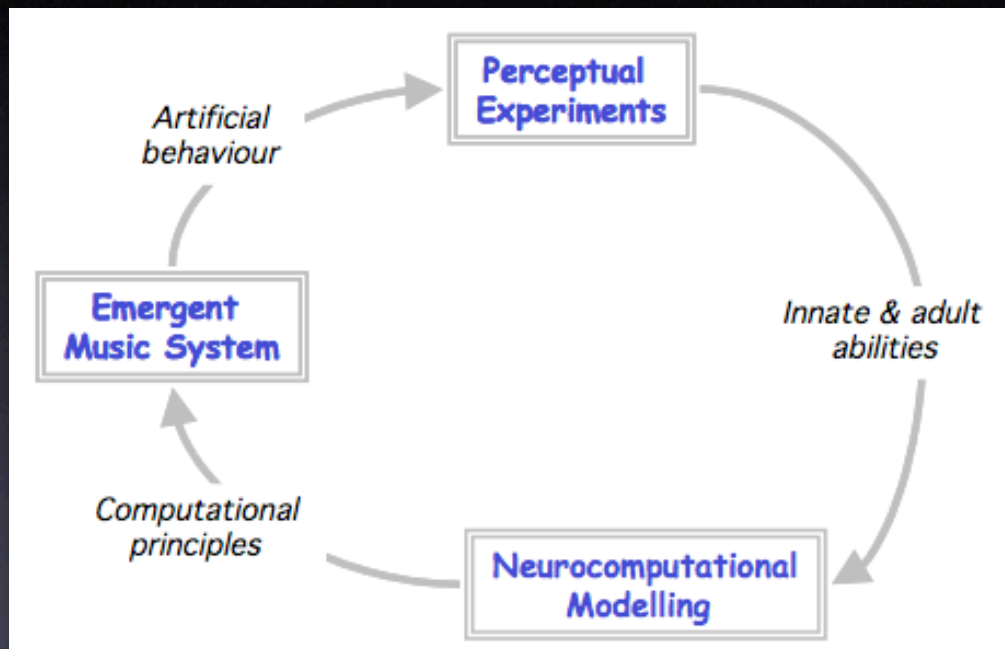
- Neuroimaging innate vs. learned auditory functions.
- Perception of musical form.
- Prefrontal cortical function controlling attention and STM.
- Spectrotemporal response fields in the thalamocortical system.
- Perception and categorisation of rhythmic patterns.
- Active perception, relative pitch and emergence of tonality.
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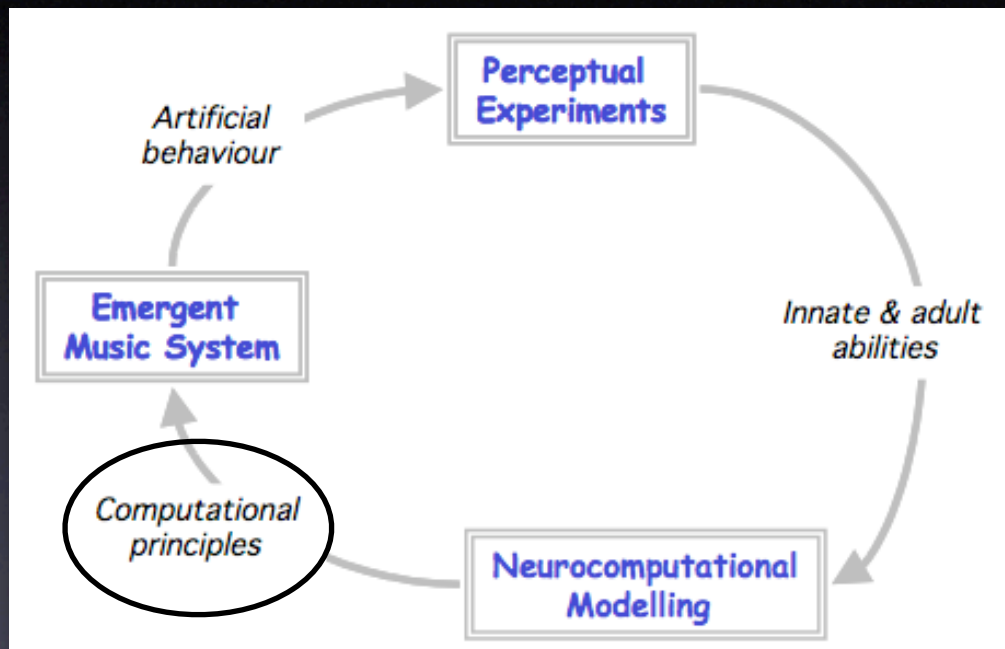
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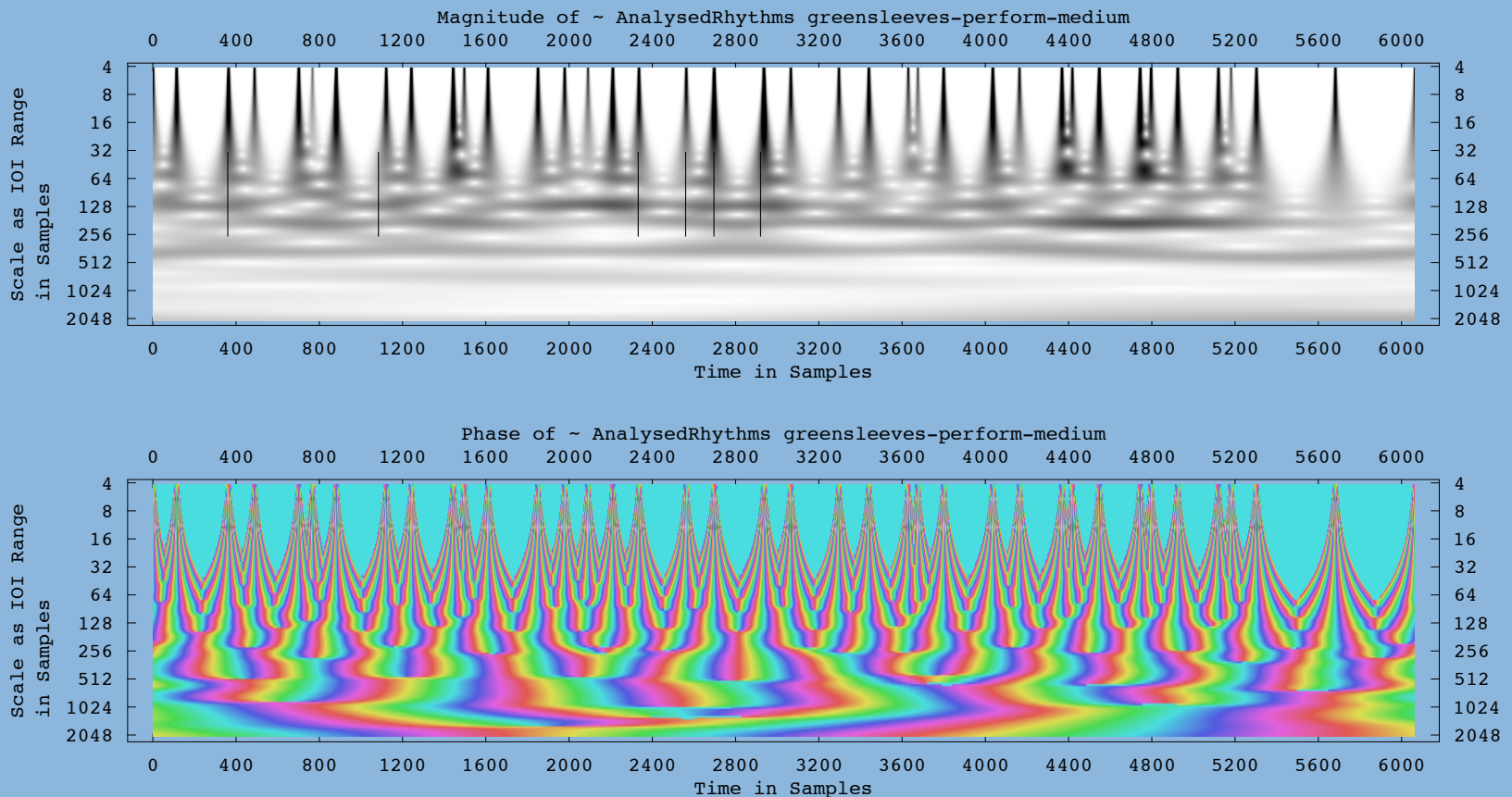


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My Research

- Computational modelling of rhythmic expectancy using *wavelet analysis*.

“Greensleeves”



Past Lives...



...with hair...

...in infrared at Comp. Sci. robotics &
vision lab at
Uni. of Western Australia...



Music and Probability

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- Why consider the two disciplines together?



Composition

- Historically, there is a long tradition of composers using chance and automation in composition.
- For example:
 - Guido d'Arezzo (1094) method of chant generation.
 - Serialism (Schoenberg, Webern, Berg, Babbitt, Carter) (1911).
 - W.A. Mozart's musical dice game (*Musikalisches Würfelspiel*, 1787).

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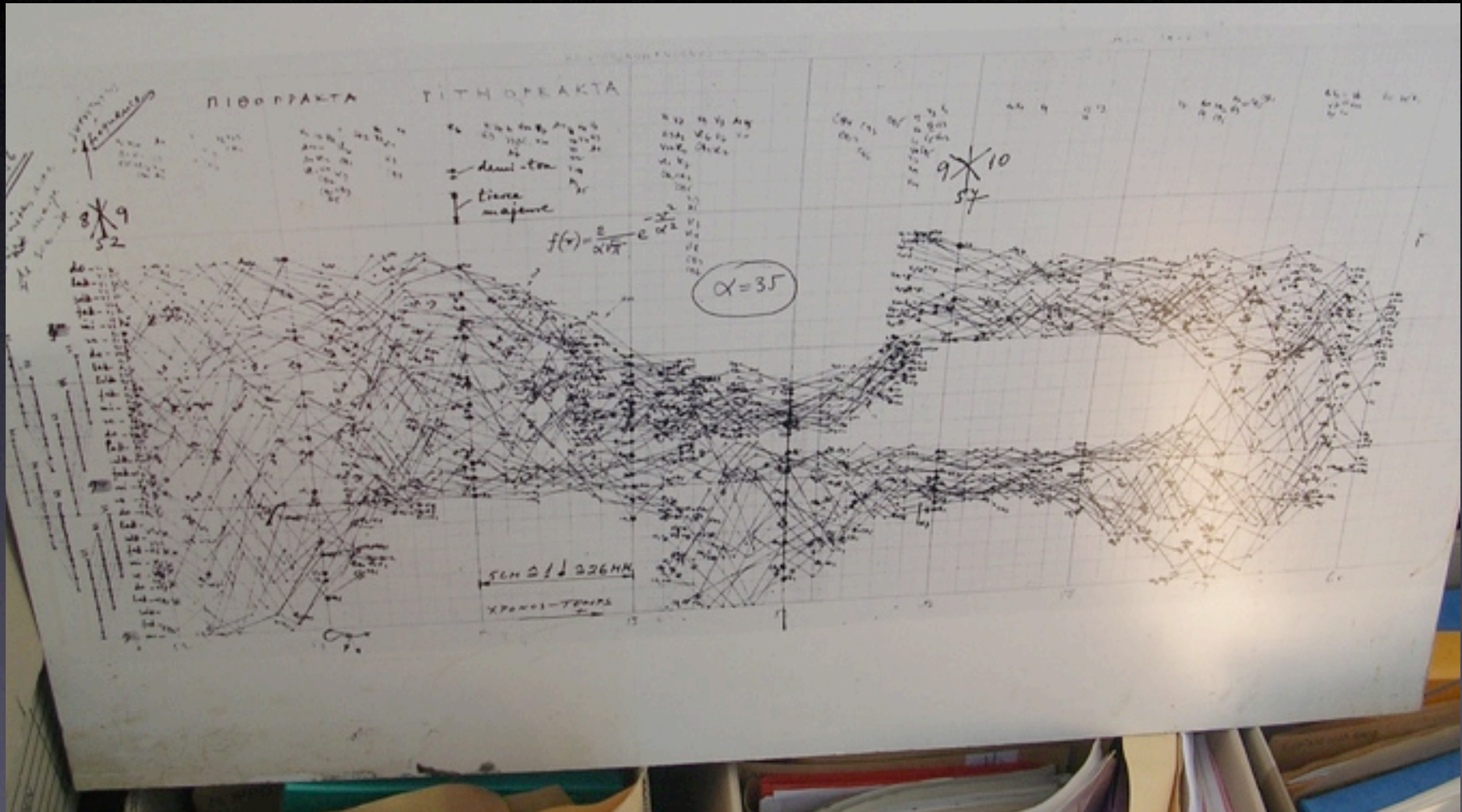


Iannis Xenakis

- Used statistical distributions to describe larger scale musical forms, to decide the selection of each note.
- “Formalised Music” Indiana University Press, 1971.



Pithoprakta (1956)



“Akrata” (1964-5)

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- ST-X Ensemble conducted by C.Z. Bornstein 1996,
Mode Records

Recent Applications

- Computer composition (Hiller & Isaacson 1959).
- Computer accompaniment (Winkler 1998).
- Improving musician/software interaction (Rowe 2001).
- Computer collaboration in improvisation.
 - e.g. STEIM <http://www.steim.nl>
- Musical games.
- Music accompaniment to computer games.
 - Reacting to a dynamically changing game context.
- Dance and Music interaction (e.g. Merce Cunningham).

Music Analysis

- Probabilistic models have been applied to various musical applications.
- Common analyses:
 - Melody
 - Rhythm

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- **Probability:** Enables quantifying the confidence of a decision or conclusion.

Examples of Uses

- **Coin/dice tossing:**
 - e.g Is the coin fair (balanced)?
- **Sampling for quality:**
 - e.g picking a bunch of fruit at the market, or products off an assembly line to assess the quality of many more.
- **Risk assessment:**
 - e.g financial speculation, medical diagnosis etc.
- **Interpretation of experimental results.**

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- Can be considered as percentage chance of occurrence.

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- $P(X = 3) = 1/6$.

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- $12 = '6' \ \& \ '6'$
 - \Rightarrow 1 in 6 chance (first throw) **and**
 - 1 in 6 chance (second throw)

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- $1/36 = 2.77\%$ likely.

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- $P(X = 6 \cap Y = 3) + P(X = 5 \cap Y = 4) + \dots = 1/9$
- “Approximately 11.11% likely”

Probability Summary

- Demonstrated how to make simple calculations of probability of event occurrence.
- References:
 - Prob. & Statistics for Engineers & Scientists 8th Ed(Walpole, Myers & Myers 2006)
 - Music & Probability (Temperley 2007)

Homework

The image displays a musical score for a piece titled "Vivace for Lute" by A. Falckenhagen, transcribed by F. Noad. The score is written for a lute and consists of three staves of music. The key signature is G major (one sharp). The first staff begins with a forte (*f*) dynamic and a half note chord (0). The second staff features a forte (*f*) dynamic and includes first and second endings. The third staff continues the piece with various dynamics and includes first and second endings. Fingerings are indicated by numbers 1-4, and breath marks are shown as horizontal lines above notes.

Vivace for Lute, A. Falckenhagen (1697-1761), trans. F. Noad

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- Example: likelihood of words in a sentence, or notes in a melody.
- First order Markov chain: Each note is dependent only on one immediately previous note.
- Second order Markov chain: Each note is dependent on the previous two notes, etc.

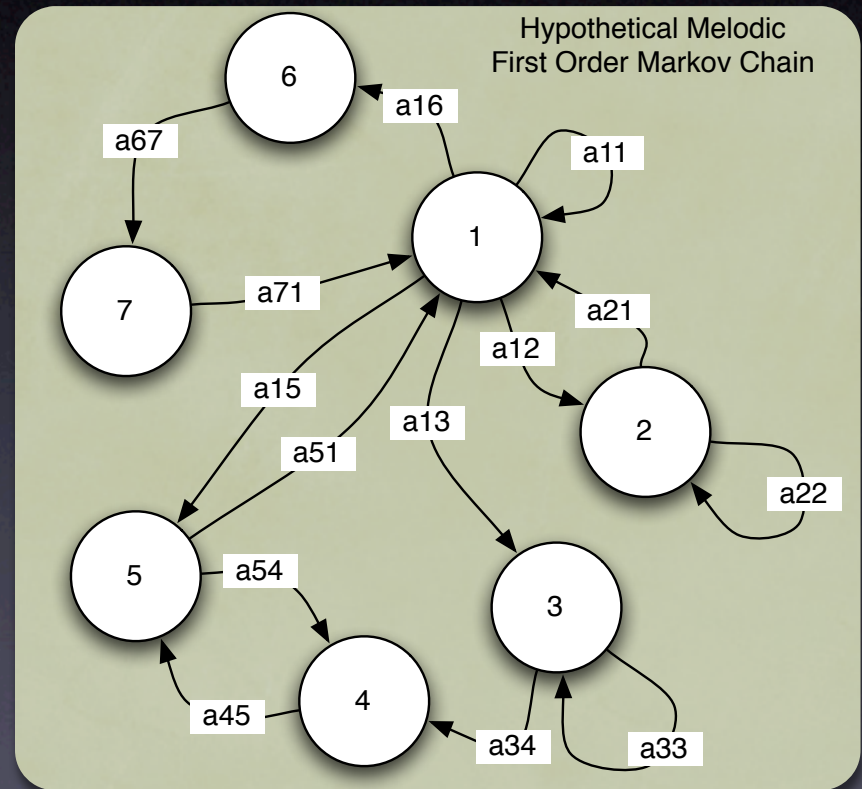
Melodic Markov Chains

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- A Markov chain is a system with n number of 'states' $S(0) \dots S(n)$, which can be scale degrees when modelling melody.

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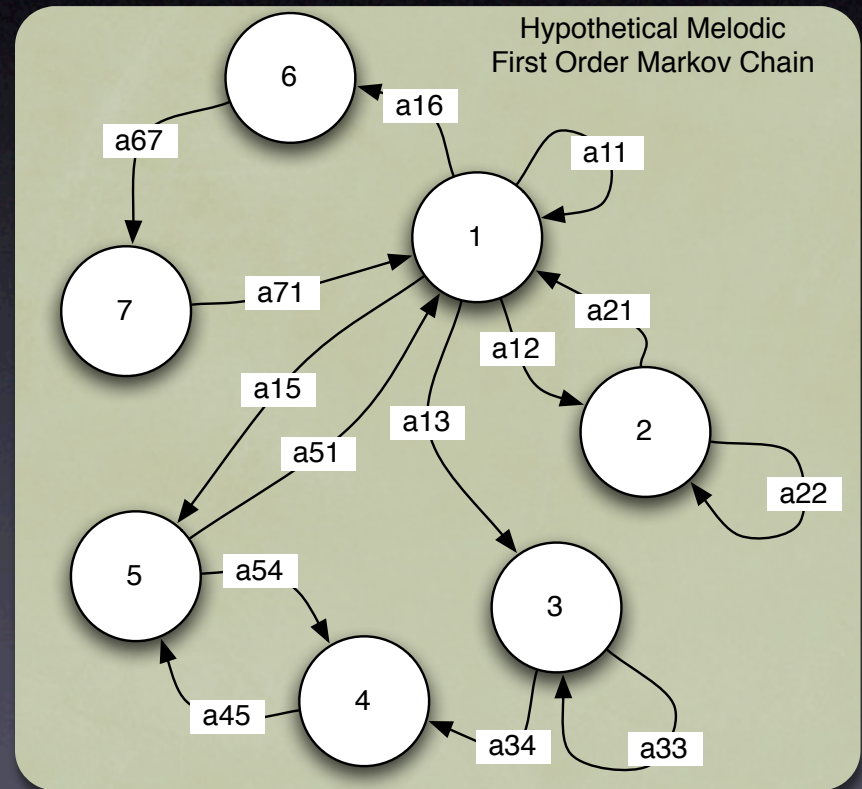
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- The state at each moment in time is specified as a probability in terms of the previous state.



First Order Markov Chain

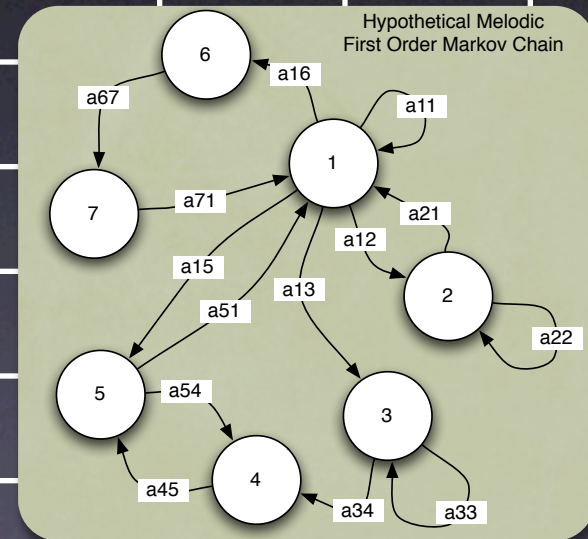
- Represents likelihood of next states (notes) in a table (matrix):

	1	2	3	4	5	6	7
1	0.1	0.3	0.1		0.3	0.2	
2	0.7	0.3					
3			0.5	0.5			
4					1.0		
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- The Markov chain is used to generate a melody by deciding which next note to choose from all possible options with a random number generator.

Markov Chain Demo

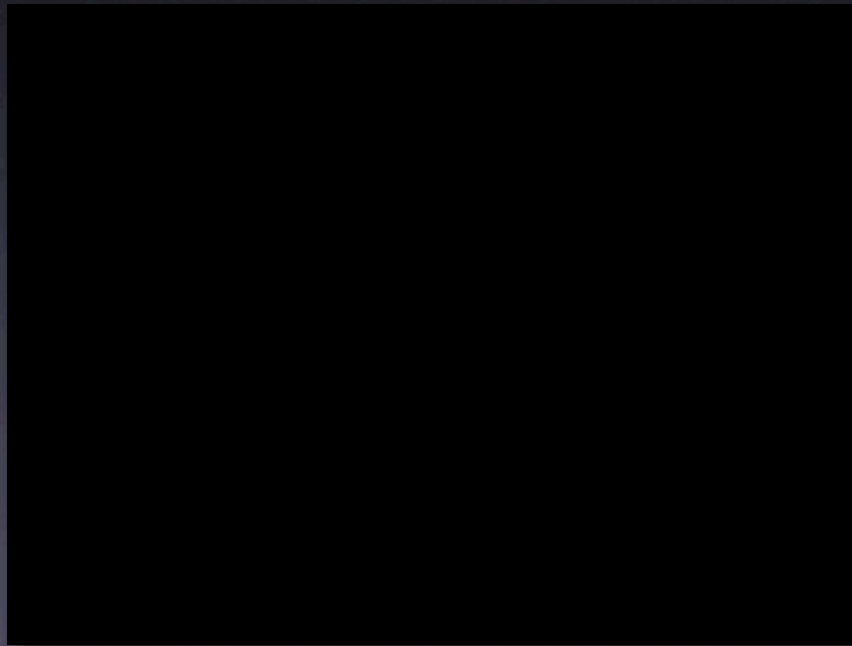
- Example modified from David Cope's "Experiments in Musical Creativity" project.
 - <http://arts.ucsc.edu/faculty/cope/>

The Continuator

- Markov melodic improviser (Pachet 2003):

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Claude Barthelemy
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- Uses Bayesian probabilistic models.

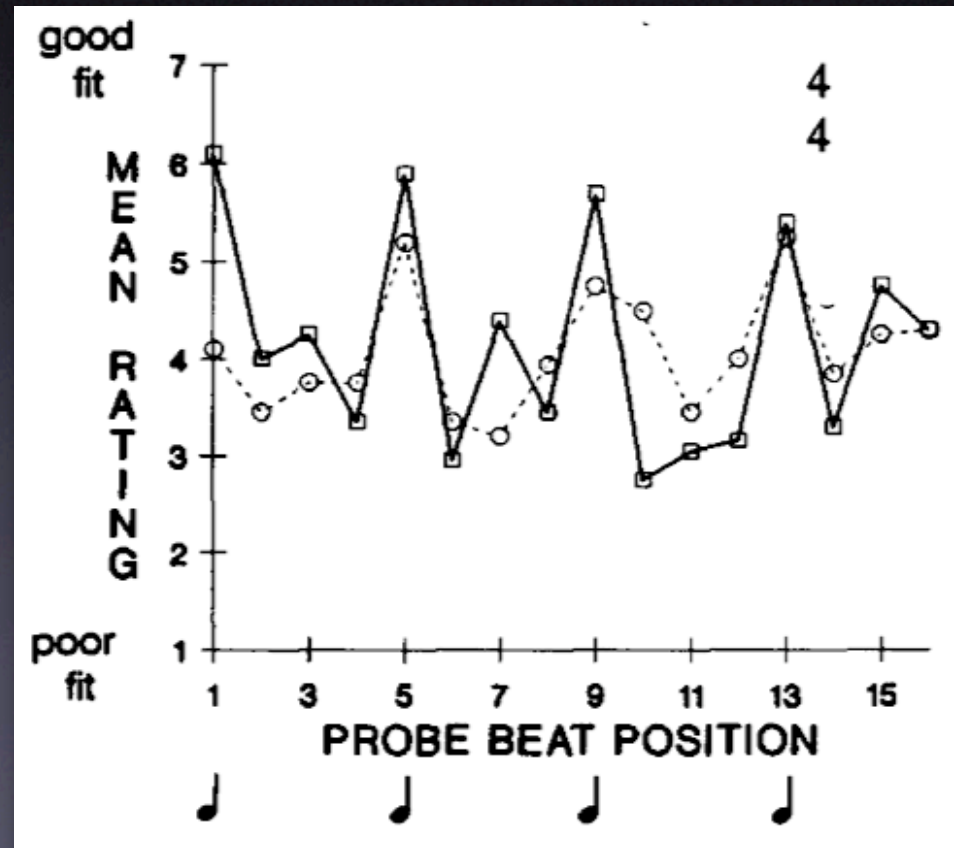
Palmer & Krumhansl

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 - Following context beats, presented probe beats and judged for goodness of fit.

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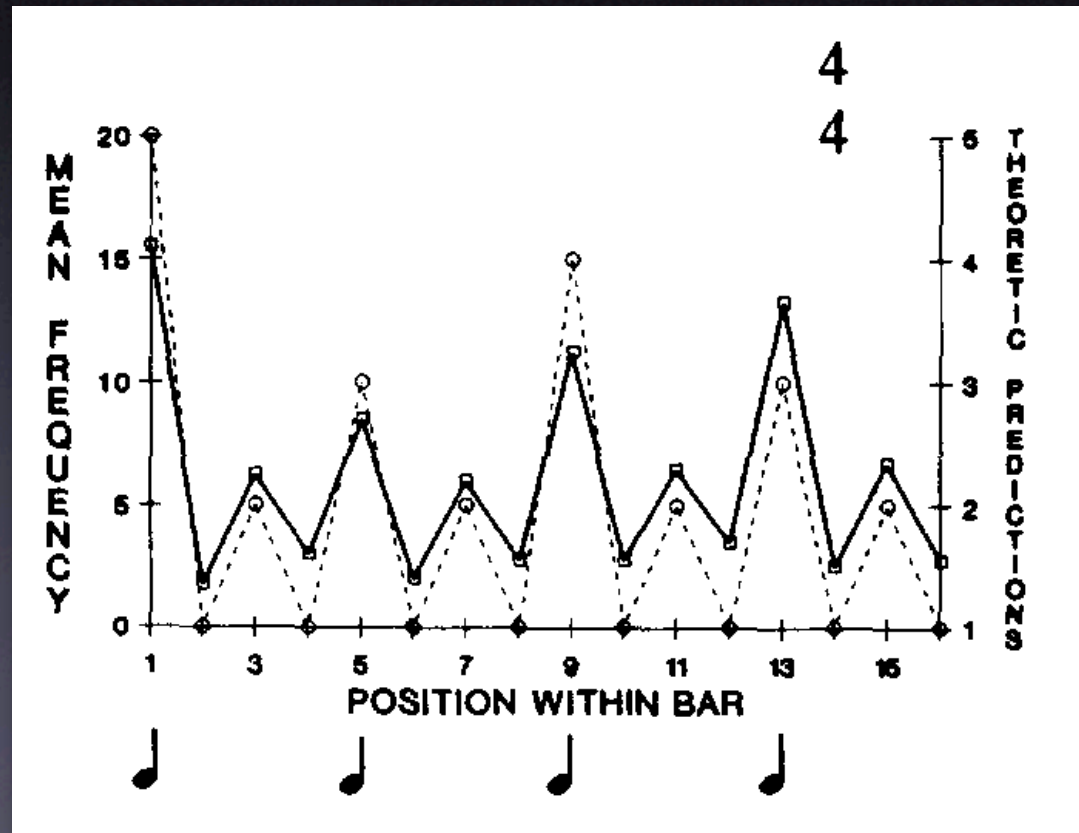
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From Palmer & Krumhansl (1990). Mean goodness-of-fit ratings for musicians (solid line) and nonmusicians (dashed line).

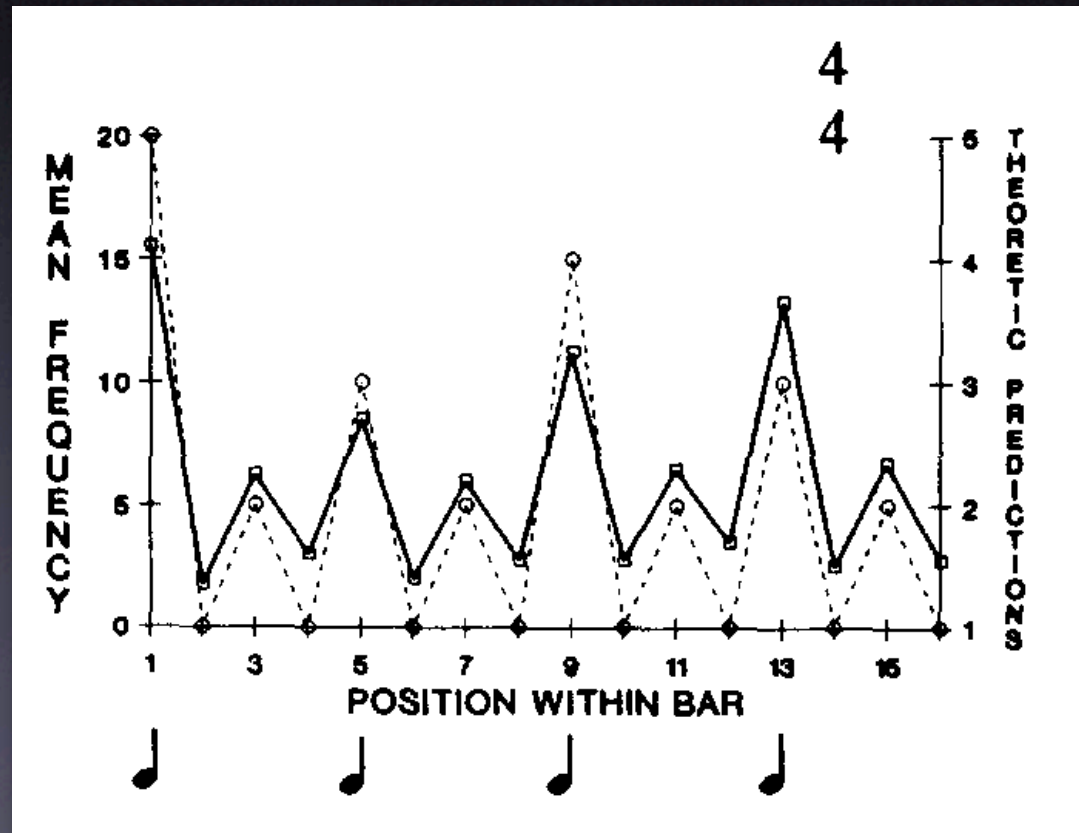
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From Palmer & Krumhansl (1990). Mean frequency counts (solid line) vs. theoretical metrical hierarchy (dashed line).

Rhythmic Markov Models

- Exercise: How would a rhythmic Markov chain be constructed? What would be an appropriate order?

Assignment

- 1) What is the most funky piece of music you know?
 - 1) Bring it, and write down the artist, title, album and year of the piece.
 - 2) Describe in a half A4, why you consider this piece funky, and what are the features that make it funky (i.e. rhythmical structure, sounds, instruments, timing, etc.)
- 2) Find two pieces of music, one that swings and one that doesn't. The swinging song does not have to be a typical jazz song, any song with triplet subdivision as metrical grid will do (this is frequently referred to as shuffle as well).
 - 1) Bring them, and write down the artist, title, album and year of the pieces.
 - 2) Describe in a half A4 why the first song swings and the second doesn't.
- 3) Read Honing & Haas (2008). It will help in doing question 2. Prepare questions to bring forward in class (N.B. These do not have to be sent in before-hand).

References

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- L. Austin. An interview with John Cage and Lejaren Hiller. *Computer Music Journal*, 16(4):15–29, 1992.
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